

**UNIVERSITY COLLEGE TATI (UC TATI)****FINAL EXAMINATION QUESTION BOOKLET**

COURSE CODE	: BET 2023
COURSE	: DIGITAL SYSTEM
SEMESTER/SESSION	: 1-2024/2025
DURATION	: 3 HOURS

**Instructions:**

1. This booklet contains **4** questions. Answer **ALL** questions.
2. All answers should be written in answer booklet.
3. Write legibly and draw sketches wherever required.
4. If in doubt, raise up your hands and ask the invigilator.

**DO NOT OPEN THIS BOOKLET UNTIL YOU ARE TOLD TO DO SO**

**THIS BOOKLET CONTAINS 8 PRINTED PAGES INCLUDING COVER PAGE**

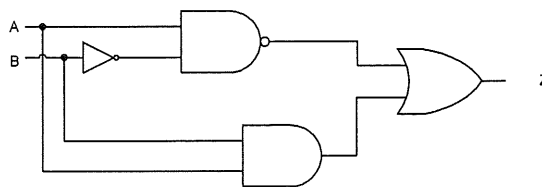
**QUESTION 1**

- a) Electronic systems can be divided into two broad categories, which are digital and analog. Answer the following questions.
- i. Define analog and digital signals. (2 marks)
  - ii. Draw the waveform of analog and digital signals. (2 marks)
- b) List **TWO (2)** types of number systems used in digital signals. (2 marks)
- c) Convert the following number systems to hexadecimal numbers. Write your answers up to two decimal places and show the working method.
- i.  $198.33_{10}$  (4 marks)
  - ii.  $1001010.11001_2$  (4 marks)
- d) Convert the decimal number of  $147_{10}$  to:
- i. Binary number. (4 marks)
  - ii. Binary coded decimal (BCD). (2 marks)

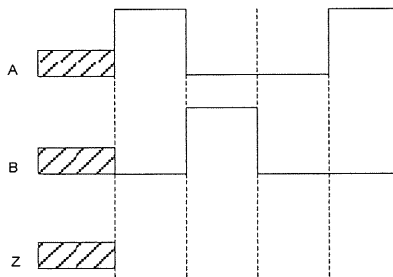
**QUESTION 2**

- a) Answer the following questions:
  - i. Draw the logic symbol for AND gate. (1 mark)
  - ii. Produce the truth table for AND gate. (2 marks)

- b) Refer to Figure 1. Complete the output timing diagram Z, in Figure 2, with A and B as the input signal. (Answer this question in the given answer booklet). (4 marks)



**Figure 1**

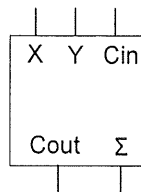


**Figure 2**

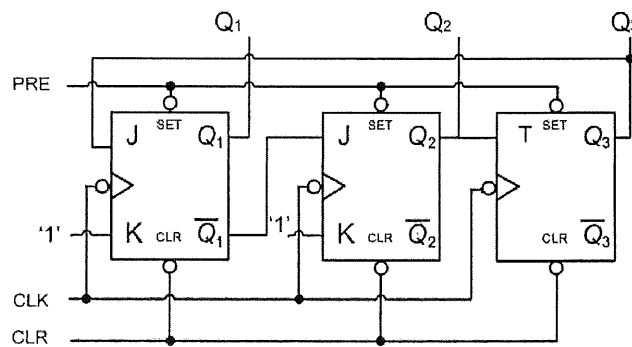
- c) For the Boolean expression below.
 
$$X(D, E, F, G) = DF + \bar{D}EFG + D\bar{E}F + \bar{E}FG$$
  - i. Produce the standard sum-of-products (SOP) expression for output X. (4 marks)
  - ii. Produce the simplified output expression X using K-Map. (6 marks)
  - iii. Draw the logic circuit for the simplified Boolean expression obtained in question 2c)ii. (4 marks)

**QUESTION 3**

- a) List **THREE (3)** examples of combinational logic devices. (3 marks)
- b) Refer to the full adder shown in Figure 3.
- Construct a 4-bit adder using the full adder. (4 marks)
  - Show the logic state of each input and output if  $X=1101_2$  and  $Y=1110_2$  for the 4-bit adder developed in question 3b)i. (4 marks)

**Figure 3**

- c) Construct the Boolean expression of  $F(A,B,C)=\sum m(0,2,5,6)$  using a 4 to 1 multiplexer. (10 marks)
- d) Figure 4 shows a synchronous sequential circuit. Complete the timing diagram in Figure 5 by drawing the waveform of signals  $Q_3$ ,  $Q_2$  and  $Q_1$ . (9 marks)

**Figure 4**

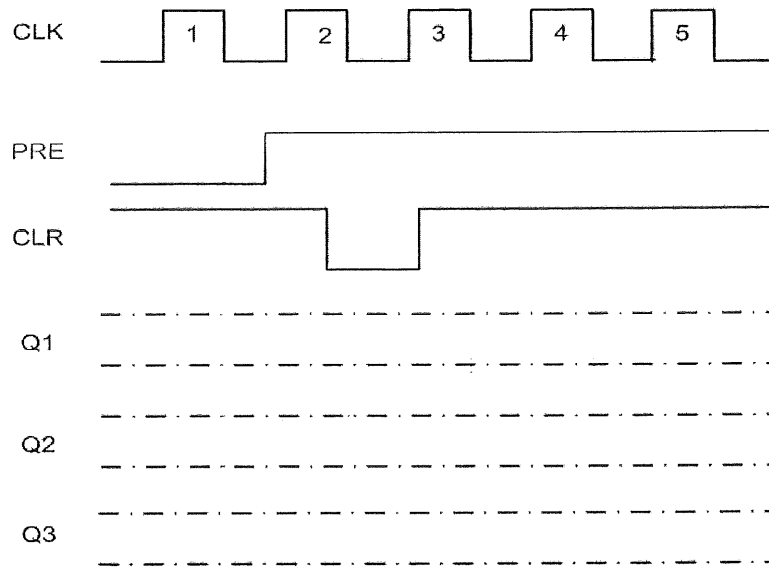
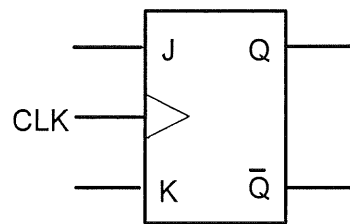
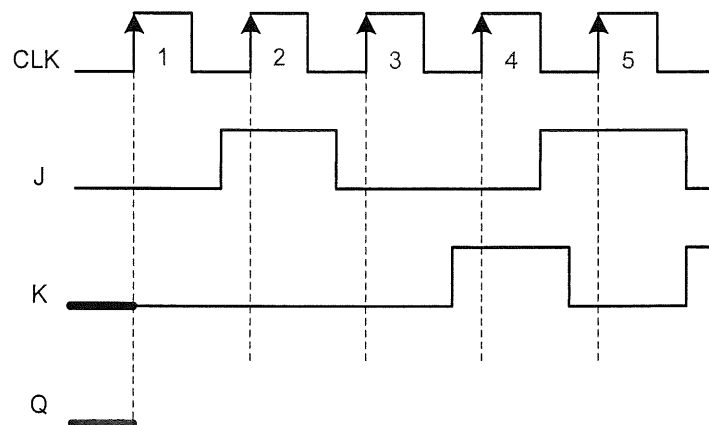


Figure 5

**QUESTION 4**

- a) List **THREE (3)** advantages of digital systems. (3 marks)
- b) List **FOUR (4)** types of shift register (4 marks)
- c) Draw movement of data for serial in serial out (SISO) shift register using D Flip Flop. (3 marks)
- d) Figure 6 shows a logic symbol for JK Flip Flop. Complete the timing diagram in Figure 7 by drawing the output waveform of signal Q. (5 marks)

**Figure 6****Figure 7**

- e) A synchronous counter with the counting sequence as shown in Figure 8 is designed by using JK flip-flops. Assume all unused states are forced to don't care condition.
- Complete the excitation table in Table 1. (Answer this question in the given answer booklet). (4 marks)
  - Produce the simplified Boolean equation for  $J_A$ ,  $K_A$ ,  $J_B$ ,  $K_B$ ,  $J_C$  and  $K_C$  using K-map. (6 marks)
  - Draw the logic circuit based on the simplified Boolean expression obtained in question 4e)ii using the positive edge triggered JK flip-flop circuit with active high clock and other suitable logic gates. (4 marks)

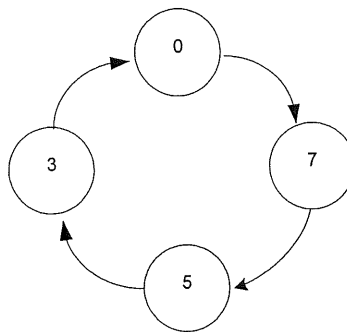


Figure 8

Table 1

PRESENT STATE			NEXT STATE			$J_A$	$K_A$	$J_B$	$K_B$	$J_C$	$K_C$
A	B	C	A'	B'	C'						
0	0	0									
0	0	1									
0	1	0									
0	1	1									
1	0	0									
1	0	1									
1	1	0									
1	1	1									

-----End of Question-----

## APPENDIX 1

Table 1: Rules of Boolean Algebra

1. $A + 0 = A$	7. $A \cdot A = A$
2. $A + 1 = 1$	8. $A \cdot \bar{A} = 0$
3. $A \cdot 0 = 0$	9. $\bar{\bar{A}} = A$
4. $A \cdot 1 = A$	10. $A + AB = A$
5. $A + A = A$	11. $A + \bar{A}B = A + B$
6. $A + \bar{A} = 1$	12. $(A + B)(A + C) = A + BC$

Table 2: Excitation Table

Flip-Flop Name	Characteristic Table	Characteristic Equation	Excitation Table																																			
SR	<table border="1"> <thead> <tr> <th>S</th> <th>R</th> <th><math>Q_{n+1}</math></th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>Q</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>Invalid</td> </tr> </tbody> </table>	S	R	$Q_{n+1}$	0	0	Q	0	1	0	1	0	1	1	1	Invalid	$Q_{n+1} = S + \bar{R}Q$	<table border="1"> <thead> <tr> <th><math>Q_n</math></th> <th><math>Q_{n+1}</math></th> <th>S</th> <th>R</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> <td>X</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>X</td> <td>0</td> </tr> </tbody> </table>	$Q_n$	$Q_{n+1}$	S	R	0	0	0	X	0	1	1	0	1	0	0	1	1	1	X	0
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